



# Vector Mechanics for Engineers: Dynamics Introduction Dynamics includes: *Kinematics*: study of the geometry of motion. Kinematics is used to relate displacement, velocity, acceleration, and time without reference to the cause of motion, i.e. forces are not considered. *Kinetics*: study of the relations existing between the forces acting on a body, the mass of the body, and the motion of the body. Kinetics is used to predict the motion caused by given forces or to determine the forces required to produce a given motion. *Newton's laws:*F = 0

- 2. F = ma
- 3. Action-reaction





































velocity of collar A is 12 in./s as it passes L, determine the change in

elevation, velocity, and acceleration

of block B when block A is at L.

• Differentiate motion relation twice to develop equations for velocity and acceleration of block *B*.

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# Vector Mechanics for Engineers: Dynamics

Sample Problem 11.12



Rotation of the arm about O is defined by  $\theta = 0.15t^2$  where  $\theta$  is in radians and tin seconds. Collar B slides along the arm such that  $r = 0.9 - 0.12t^2$  where r is in meters.

After the arm has rotated through  $30^\circ$ , determine *(a)* the total velocity of the collar, *(b)* the total acceleration of the collar, and *(c)* the relative acceleration of the collar with respect to the arm.

## SOLUTION:

- Evaluate time *t* for  $\theta = 30^{\circ}$ .
- Evaluate radial and angular positions, and first and second derivatives at time *t*.
- Calculate velocity and acceleration in cylindrical coordinates.
- Evaluate acceleration with respect to arm.

Contract the problem of the proble









# Vector Mechanics for Engineers: Dynamics

# Sample Problem 11.4



Ball thrown vertically from 12 m level in elevator shaft with initial velocity of 18 m/s. At same instant, open-platform elevator passes 5 m level moving upward at 2 m/s.

Determine (*a*) when and where ball hits elevator and (*b*) relative velocity of ball and elevator at contact.

## SOLUTION:

- Substitute initial position and velocity and constant acceleration of ball into general equations for uniformly accelerated rectilinear motion.
- Substitute initial position and constant velocity of elevator into equation for uniform rectilinear motion.
- Write equation for relative position of ball with respect to elevator and solve for zero relative position, i.e., impact.
- Substitute impact time into equation for position of elevator and relative velocity of ball with respect to elevator.

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